# Composite Hierarchical Pitch Angle Control for a Tidal Turbine Based on the Uncertainty and **Disturbance Estimator**

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Abstract—With the fast development of tidal turbines for sustainable energy generations, reliable and efficient tidal pitch systems are highly demanded. This paper presents a systematic design for a novel tidal pitch system based on hydraulic servo and bevel geared transmission. This system holds the characteristics of compact and triangular structure, making it easy to be installed in a narrow turbine hub. The pitch system dynamics are modeled by taking account of model uncertainties and external disturbances. An uncertainty and disturbance estimator (UDE)-based robust pitch control algorithm is developed to achieve effective pitch angle regulation, disturbance rejection, and generator power smoothing. The UDE controller is designed in a composite hierarchical manner that includes an upper level power smoothing controller and a low-level pitch angle tracking controller. The performance of the proposed pitch system and the UDE control is demonstrated through extensive simulation studies based on a 600-kW tidal turbine under varying tidal speeds. Compared with the conventional controller, the UDE-based pitch controller can achieve more reliable power smoothing and pitch angle tracking with higher accuracy.

Index Terms—Pitch angle tracking, pitch system, power smoothing, tidal turbine, uncertainty and disturbance estimator (UDE)-based pitch control.

#### NOMENCLATURE

$oldsymbol{A}_m \in \Re^{3  imes 3} \ oldsymbol{B}_m \in \Re^{3  imes 1}$	Constant matrices of the reference model.	g( G
$egin{aligned} &oldsymbol{A}_p \in \Re^{3  imes 3}, \ &oldsymbol{B}_p \in \Re^{3  imes 1}, \ &oldsymbol{C}_p \in \Re^{3  imes 1} \end{aligned}$	State matrices of the hydraulic pitch servo.	$g_f \ g_eta \ i_p$
$oldsymbol{B}_n^+$	Moore–Penrose inverse of $B_p$ .	Í
b	Known control gain.	$J_b$
$\hat{b}$	Control gain estimate.	$J_g$
$\tilde{b}$	Estimation error $\tilde{b} = b - \hat{b}$ .	$J_n$
		$J_t$

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$b_L$	Equivalent viscous damping coefficient	
	in the geared transmission.	
$b_{ls}$	Damping ratio of the low-speed side.	
$b_{\beta}$	Known control gain for the pitch angle.	
c(t)	Piecewise uniformly and continuous	
	bounded command.	
$C_p$	Power coefficient of the tidal turbine.	
$c_1 - c_6$	Coefficients for calculating $C_p$ .	
$c_m$	Total leakage coefficient of the	
	hydraulic pitch servo.	
C(s)	Laplace transforms of $c(t)$ .	
d(x,t)	Lumped nonaffine term including	
	uncertainties and disturbances.	
$d_n(t)$	Lumped uncertain and disturbance	
$P \land I$	term.	
$\hat{d}_n(t)$	Estimate of $d_n(t)$ .	
$d_{\beta}$	Lumped unknown disturbance and	
p	model uncertainties.	
$D_m$	Constant displacement of the hydraulic	
m	motor.	
$\boldsymbol{e}_{n}(t)$	Pitch angle tracking error.	
$E_{n}(s)$	I analce transforms of $e_{-}(t)$	
p(0)	Bounded nitch angle deviation or track-	
υρ	ing error	
a(r)	Known smooth nonlinear function	
$G_{\alpha}(s)$	Strictly proper stable low pass filter	
$a_f(t)$	Impulse response of the filter $G_{\ell}(s)$	
$g_f(v)$ $g_a(w, v, \beta)$	Known smooth nonlinear function	
$i_{\mu}$	Revel gear transmission ratio	
$I \in \Re^{3 \times 3}$	Identity matrix	
	Inertia of the turbine blades	
	Inertia of the generator	
J.	Pitch servo side inertia	
	Turbine rotational inertia	
$\mathbf{K}_{2} \in \Re^{3 \times 3}$	Fror feedback gain matrix	
$K_{2} \subset \mathcal{H}$	Ellow-pressure coefficient	
k,	Fourivalent spring stiffness	
$k_{ls}$	Damping coefficient of the high speed	
ng	shaft	
K	Ditch serve value flow gain coefficient	
K K	Constant proportional mapping asin	
la la	Domping coefficient	
$\kappa_t$	Damping coefficient.	
$L \stackrel{\uparrow}{=} \{\bullet\}$	Inverse Laplace operation of $\bullet$ .	

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Р	Adequately selected positive definite
	matrix.
$p_L$	Load pressure of the hydraulic pitch
	servo.
$q_L$	Hydraulic load flow rate.
R	Tidal turbine blade radius.
S	Laplace operator.
$T_e$	Magnetic reaction torque of the
	generator.
$T_h$	High speed shaft torque.
$T_L$	Low-speed shaft side reaction torque.
$T_m$	Torque from the hydraulic pitch servo.
$T_p$	Total inertia moment acting on the tur-
	bine blades.
v	Effective tidal stream speed.
$V_1(t), V_2(t)$	Lyapunov function candidates.
$V_n$	Total motor volume of the hydraulic
Γ	pitch servo.
x	State variable of generator power.
$x_m$	Reference state vector.
$\boldsymbol{x}_{m}$	State vector of the hydraulic pitch
$\omega_p$	servo
$\mathbf{X}$ (s)	Laplace transform of $r$
r p(0)	Pitch servo valve spool displacement
$\frac{x_v}{\beta}$	Tidal blade pitch angle
B	Hydraulic fluid's effective volume elas-
$\rho_e$	tigity modulus
ß	Pafaranca pitch angle control input
$\rho_r$	Reference pitch angle control input.
× 1, 1, 12	Linmodeled dynamics and nerematric
$o_m$	uncertainties
	uncertainties. Security $(1025 \text{ kg/m}^3)$
$\rho$	Seawater density (1023 kg/m <sup>2</sup> ).
$\theta_t$	Angular deviation of the turbine rotor.
$\theta_{ls}$	Angular deviation of the low speed
0	shaft.
$ heta_m$	Rotation angle of the servo side bevel
	gear.
λ	Tidal turbine tip speed ratio (TSR).
$\lambda_i$	Intermediate variable.
$\lambda_{\min}(\bullet)$ and $\lambda_{\max}(\bullet)$	Minimum and maximum eigenvalues
	of the given matrix $\bullet$ .
au	Small time constant.
$\omega_{ls}$	Angular rotation speed of the low speed
	shaft.
$\omega_g$	Rotation speed of the generator.
$\omega_t$ .	Rotation speed of the turbine rotor.
$\Delta d_p = d_p(t) - \hat{d}_p(t)$	Estimation error of the lumped distur-
	bance term $d_p(t)$ .
●	Matrix Frobenius norm for a given
	matrix•.
*	Convolution operator.

## I. INTRODUCTION

S A promising renewable energy source with high predictability, tidal energy is gaining increased attention and is becoming more and more competitive with other energy sources, such as wind, wave, and solar, in terms of resource availability, supply security, and reliability. Tidal turbines exploit tidal stream flows directly without the need of large civil engineering structures to build up a water head. Their design and development have increased significantly in recent years. A number of full-scale turbine prototypes have been developed or are scheduled to be deployed, such as the 300-kW marine current turbine (MCT) technology, the 1 MW twin rotor system in the U.K. [1], the contra-rotating 500-kW TidEl turbines [2], the DeltaStream turbine [3], and the Lunar Energy tidal turbine [4].

However, the harsh and highly turbulent working conditions pose a major challenge to the tidal turbines regarding the reliability, effectiveness, and survivability. Thus, advanced technologies or subsystems that can effectively tackle these problems, which, therefore, reduce tidal turbines' operation and maintenance costs, are of significant importance. One such subsystem is the blade pitch system which has been widely used in modern wind turbines [5], [6] and has been proven to be a reliable and cost-effective technology for power smoothing and load mitigation. Similarly, tidal turbines can benefit from pitch control. The pitch system can pitch the blades to fully utilize bidirectional tidal flows, to limit power generations when the tidal speed is above rated and to achieve hydrodynamic stall in case of emergency. However, so far very few studies have been conducted on the pitch systems of tidal turbines while pitch system technology of wind turbines is not suitable to be directly applied for tidal turbines due to inherent differences of both systems, e.g., different stall and loading characteristics since seawater is about 800 times denser than air.

A hydraulic pitch control mechanism was described in [7] for a straight-bladed Darrieus-type vertical-axis tidal turbine. The movement of the pitch mechanism is of sinusoidal shape and is continuously variable in amplitude. The blade pitch actuation is powered by the turbine's own rotation and is thus passively regulated. In [8] and [9], a collective pitch system was designed for tidal turbine using a rack and pinion gear set and hydraulic drive to provide an available blade pitch angle. Then a reduced variation pitch control strategy was proposed based on tidal current velocity preview to reduce pitch actions and extend the tidal turbine's working life. Comparative results validated the significant reductions of pitch actions and relatively high efficiency for energy generation. In [10], a pitch angle controller for a variable-speed tidal turbine was developed and the performance comparison between the pitch regulated tidal turbine and a stall regulated tidal turbine was examined in MATLAB under turbulent tidal flows. The results indicated that the pitch regulated turbine was a more attractive solution for turbine developers. The rack and pinion set is a conveniently used mechanism to convert rotary motions into linear motions and vice versa, holding the advantages of being cheap and compact. However, the most adverse disadvantages of rack and pinion would be the inherent frictions and low mass moment of inertia since the rack and pinion can only work with certain levels of friction and will be subject to wear more than usual during longtime linear and rotary motion transformations [11]. Thus, for the rack and pinion type pitch systems, the motion transformations are inevitably imprecise, leading to inaccurate pitch actuation. Some

of the existing designs of the tidal turbine pitch subsystem are bought from wind turbines which are relatively common and simple. Hence, there is a need for advanced and robust pitch system to deliver more precise pitch control actions and simultaneously take into account the particular characteristics of tidal turbines.

In this paper, a novel and effective tidal pitch system is proposed in which hydraulic servo and bevel geared transmission are employed to highly enhance the pitch control accuracy. The tidal pitch system has compact and stable structure, and is readily sized and installed into the front inner narrow space of the turbine hub. The excellent characteristic of the bevel geared transmission can also guarantee smooth and direct pitch actions. The dynamic characteristics of the pitch system are modeled and analyzed, and external loads and disturbances are also considered and integrated into the overall system model. An efficient and robust UDE-based pitch control scheme is then designed. The UDE control has been successfully applied to a wide class of linear, nonlinear uncertain systems and is easy to be implemented and tuned while offering better robust performances than the traditional control schemes [12]. It includes three inherent design freedoms: a reference model, an error feedback gain, and a filter, which enable high decoupling between reference tracking and disturbance rejection [13]. The UDE-based robust control is also able to achieve good robust performance by estimating and compensating the unknown dynamics and disturbances in a system with a filter having the appropriate frequency characteristics [14]. The UDE-based pitch control scheme is designed in a composite hierarchical manner that includes an upper level generator power smoothing controller and a low-level pitch angle tracking controller. The main contributions and novelty of this paper are highlighted as follows.

- 1) A novel and effective tidal pitch system is proposed based on hydraulic servo and bevel geared transmission.
- 2) An efficient and robust UDE-based pitch control scheme is designed in a composite hierarchical manner that includes an upper level generator power smoothing controller and a low level pitch angle tracking controller. The overall stability of the UDE pitch control is proved through Lyapunov functions.
- 3) The dynamics and control performances of the proposed pitch system and UDE pitch controller are demonstrated through extensive simulations based on a 600-kW tidal turbine under both the normal and extreme conditions.

The remainder of this paper is organized as follows. In Section II, the design of the proposed tidal pitch system is introduced. In Section III, dynamics modeling of the proposed pitch system is presented. Section IV presents the UDE-based power smoothing control of the tidal turbine. Section V presents the UDE-based pitch angle control. Section VI presents the stability analysis of the overall UDE pitch controller. Section VII presents the validations and discussions of the proposed pitch system and UDE controller. Section VIII concludes the paper.

## II. TIDAL PITCH SYSTEM

The novel tidal pitch system is designed for a general variablespeed, three-bladed, horizontal axis tidal turbine to provide



Fig. 1. Design of the novel tidal pitch system. 1—Hydraulic pitch servo. 2—Servo side bevel gear. 3—Blade side bevel gear. 4—Pitch bearing. 5—Main shaft. 6—Auxiliary support.



Fig. 2. Design of the hydraulic pitch servo.

accurate and bidirectional pitch actions based on hydraulic servo and bevel geared transmission. As illustrated in Fig. 1, the pitch system mainly consists of a hydraulic pitch servo 1, a servo side bevel gear 2, blade side bevel gears 3, pitch bearings 4, and auxiliary support 6. The hydraulic pitch servo 1 is installed in the front inner cone of the turbine hub and is rigidly connected to the servo side bevel gear 2. The three-blade side bevel gears 3 are connected to blade roots through bolts and pitch bearings 4, and are also precisely engaged with the servo side bevel gear 2. Thus, the three turbine blades can be uniformly pitched by the hydraulic pitch servo 1 through the bevel gears 2, 3, and pitch bearings 4. The blade pitch angle is determined by the rotation angle of the pitch servo and the transmission ratio of the bevel gears. The auxiliary support 6 includes some specific structures, such as waterproof sealing and housing to support the pitch system.

Since the hydraulic servo has relatively high torque/volume ratio, the pitch system can be adequately and compactly sized into the inner narrow space of the turbine hub. The pitch system is also designed as a triangular structure with large stability and a low center of gravity for operations. This design is essentially different from the aforementioned pitch systems and effectively satisfies the special requirements of fast dynamic performances, precise pitch motions, and large pitch torques of tidal turbines.

As shown schematically in Fig. 2, the hydraulic pitch servo mainly consists of a servo motor, a hydraulic pump, check valves, a servo valve, a high pressure accumulator (HPA), a low pressure accumulator (LPA), a relief valve, a hydraulic motor, and a UDE pitch angle controller. The servo motor drives the hydraulic pump to supply high pressure hydraulic oil flow, which is then routed by the check valves and the servo valve to the hydraulic motor that is rigidly connected to the bevel gears to generate pitch motions. The pump in the turbine hub is adjustable from full to a 50% flow rate, and its efficiency only slightly changes with time-varying tidal flow speeds. The accumulators, HPA, and LPA function as energy storage in terms of compressed gas to provide filter pressure pulsations and pressure compensations. The HPA is used to maintain a sufficiently high pressure in the suction ports of the hydraulic machines. The relief valve is designed for limiting the hydraulic system pressure and ensuring system safety in case of large pitch torque pulsations, by setting the safety pressure at 10-20% above the maximum operation pressure [15].

The servo valve with matched orifices is controlled by the UDE pitch controller to accurately regulate the direction, rotation angle, and speed of the hydraulic motor that consequently drives the bevel gears fixed at the blade roots to change blade pitch angles accordingly. The pitch angle controller generates control commands for the servo valve based on the feedback pitch angles and thus the blades are pitched corresponding to different tidal speed conditions. In case of emergency, the tidal turbine can be stopped by pitching the blades to feather and using high pressure flows from the HPA. The designed pitch system is robust against various exogenous disturbances due to the inherent loading balance and high pressure limitations of the hydraulic transmission.

Since the seawater density is around 800 times higher than air, generating the same amount of power requires much smaller sized tidal turbines than wind turbines. Therefore, significantly different from wind turbine pitch systems that do not stress much on turbine size to accommodate, the proposed tidal pitch system design takes into account the much smaller tidal turbine hub size. It is designed based on compact hydraulic servo and bevel geared transmission with triangular structure such that it can be adequately and compactly sized into the inner narrow space of the turbine hub. The employed hydraulic servo-based tidal pitch system not only has relatively higher torque/volume ratio, but also is much sturdier than the commonly used electric motorbased pitch systems in wind turbines. In addition, this tidal pitch design makes the tidal turbine durable enough to survive the hostile underwater environment. In addition, the tidal pitch angle range is much smaller than that of wind turbines due to the much higher seawater density, which requires higher accuracies on the tidal pitch system and its control than its wind turbine counterpart.

#### **III. DYNAMICS MODELING**

The dynamics of the tidal pitch system can be modeled based on fundamental governing equations of each component in an integrated configuration. External loads and environmental conditions that can alter the operation characteristics of the pitch system will also be considered and integrated into the overall system model.



Fig. 3. Typical power coefficient curves for a tidal turbine.



Fig. 4. Schematic of the geared drivetrain.

#### A. Hydrodynamics of the Tidal Turbine

The hydrodynamic torque and tidal stream speed acting on the tidal turbine blades can be represented as

$$\begin{cases} T_t = \frac{\rho \pi R^o \omega_t^2 C_p}{2\lambda^3} \\ v = \frac{\omega_t R}{\lambda} \end{cases}.$$
(1)

As indicated in (1), the tidal turbine torque is strongly dependent on both the power coefficient  $C_p$  and tip speed ratio (TSR), which are expressed as

$$\begin{cases} C_p(\lambda,\beta) = c_1 \left(\frac{c_2}{\lambda_i} - c_3\beta - c_4\right) \exp(-\frac{c_5}{\lambda_i}) + c_6\lambda \\ \lambda_i = \frac{1}{\lambda + 0.08\beta} - \frac{0.035}{\beta^3 + 1} \end{cases}$$
(2)

where the constant coefficients  $c_1-c_6$  are:  $c_1 = 0.5176$ ,  $c_2 = 116$ ,  $c_3 = 0.4$ ,  $c_4 = 5$ ,  $c_5 = 21$ , and  $c_6 = 0.0068$ .

The  $C_p(\lambda, \beta)$  characteristics for different values of the pitch angle  $\beta$  are shown in Fig. 3, which implies that the maximum value of  $C_p$  ( $C_{p \max} = 0.4798$ ) is achieved when  $\beta = 0^{\circ}$  and  $\lambda = 8$ . With the increasing pitch angle from 0° to 15° and TSR from 0 to 9, the power coefficient decreases from 0.48 to around 0.1. Hence the turbine power generations can be readily regulated at stable values by maintaining the optimal blade pitch angle when the tidal stream is above rated speed.

#### B. Tidal Turbine Drivetrain

As the turbine rotor spins, the mechanical energy of the rotor is transmitted via the drivetrain to the generator where the tidal energy is converted into the electricity. As illustrated in Fig. 4, the equivalent geared drivetrain of the tidal turbine consists of a small mass and a large lumped mass that represent the inertias of the generator rotor and the turbine rotor. A geared transmission with ratio  $i_g$  is placed between the masses for increasing the turbine speed and decreasing the torque. The turbine side dynamics is represented as

$$\begin{cases} J_t \dot{\omega}_t = T_t - k_t \omega_t - T_L \\ T_L = k_{ls} \left( \theta_t - \theta_{ls} \right) + b_{ls} \left( \omega_t - \omega_{ls} \right) \end{cases}$$
(3)

The generator side dynamics is represented as

$$J_g \dot{\omega}_g = T_h - k_g \omega_g - T_e.$$
(4)

The geared transmission that links the low speed shaft and high speed shaft can be described as

$$\begin{cases} T_L \omega_{ls} = T_h \omega_g \\ \frac{\omega_g}{\omega_{ls}} = \frac{T_L}{T_h} = i_g \end{cases}$$
(5)

Considering (3) and (5), the turbine rotation speed is

$$\begin{cases} \omega_t = \Delta \omega_t + \omega_{ls} = \Delta \omega_t + \frac{\omega_g}{i_g} \\ \Delta \omega_t = \omega_t - \omega_{ls} \end{cases}$$
(6)

Substituting (5) and (6) into (3) gives

$$J_t\left(\Delta\dot{\omega}_t + \frac{\dot{\omega}_g}{i_g}\right) = T_t - k_t\omega_t - T_h \cdot i_g.$$
(7)

Substituting  $T_h = J_g \dot{\omega}_g + k_g \omega_g + T_e$  from (4) into (7) gives

$$\dot{\omega}_{g} = \frac{i_{g}}{J_{t} + J_{g}i_{g}^{2}}T_{t} - \frac{(k_{t} + k_{g}i_{g}^{2})}{J_{t} + J_{g}i_{g}^{2}}\omega_{g} - \frac{i_{g}^{2}}{J_{t} + J_{g}i_{g}^{2}}T_{e} - \frac{i_{g}(k_{t}\Delta\omega_{t} + J_{t}\Delta\dot{\omega}_{t})}{J_{t} + J_{g}i_{g}^{2}}.$$
(8)

Substituting (1) and (2) into (8) and rearranging the resulting equations yield

$$\begin{split} \dot{\omega}_{g} &= g_{\beta} \left(\omega_{g}, \beta\right) = \frac{\rho \pi R^{5} \omega_{t}^{2} i_{g}}{2\lambda^{3} \left(J_{t} + J_{g} i_{g}^{2}\right)} \left[ c_{1} \left(\frac{c_{2}}{\lambda_{i}} - c_{4}\right) \exp(-\frac{c_{5}}{\lambda_{i}}) + c_{6} \lambda \right] \\ &- \frac{\left(k_{t} + k_{g} i_{g}^{2}\right)}{J_{t} + J_{g} i_{g}^{2}} \omega_{g} - \frac{i_{g}^{2}}{J_{t} + J_{g} i_{g}^{2}} T_{e} \\ &b_{\beta} &= -\frac{\rho \pi R^{5} \omega_{t}^{2} i_{g} c_{1} c_{3} \exp(-\frac{c_{5}}{\lambda_{i}}) i_{g}}{2\lambda^{3} \left(J_{t} + J_{g} i_{g}^{2}\right)} \\ &d_{\beta} &= -\frac{i_{g} \left(k_{t} \Delta \omega_{t} + J_{t} \Delta \dot{\omega}_{t}\right)}{J_{t} + J_{g} i_{g}^{2}} \end{split}$$
(10)

As expressed in (10), the generator torque  $T_e$  is attainable from the generator side converter regulations and is thus known for the pitch angle controller while the disturbance term  $b_\beta$ consists of shaft angle and speed deviations, which is the main source of decreasing the drivetrain transmission efficiency over a wide power range.

#### C. Bevel Geared Transmission

The dynamic torque balance equation for the bevel geared transmission is described as

$$\begin{cases} T_m = \left(J_m + \frac{J_b}{i_p^2}\right)\ddot{\theta}_m + b_L\dot{\theta}_m + \frac{T_p}{i_p}\\ \theta_m = \beta \cdot i_p \end{cases}.$$
 (11)

The actual pitch load  $T_p$  depends on the aerofoil shapes of the turbine blades and blade pitch angle, and can thus be as an out-plane torques that induce the fore-aft motions of the blades and hub. The pitch load can also be calculated by using similar equations as wind turbines [16].

#### D. Pitch Servo System

As mentioned earlier in Section II and Fig. 2, the hydraulic pitch servo system is controlled by a four-way electrohydraulic servo valve which consists of two inlet and two outlet orifices and a spool that changes the flow passage area of the outlet orifices. The control flow equation of the hydraulic servo valve for the load flow rate is written as

$$q_L = K_q x_v - K_c p_L. \tag{12}$$

The servo valve dynamics is sufficiently faster than the dynamics of the remaining parts of the system. Therefore, the servo valve opening is directly related to the control input u by a known constant proportional mapping as

$$x_v = K_u \cdot u. \tag{13}$$

The governing equation of the flow-pressure continuous model of the hydraulic motor relates the pressure differential across the hydraulic motor chambers and the passage area to the flow rate. Thus

$$q_L = D_m \dot{\theta}_m + c_m p_L + \frac{V_p}{4\beta_e} \dot{p}_L. \tag{14}$$

The active torque generated by the hydraulic motor is

$$T_m = D_m p_L + \delta_m. \tag{15}$$

The state space representation of the hydraulic wind power system is derived by combining (11)–(15) as follows:

$$\dot{\boldsymbol{x}}_p = \boldsymbol{A}_p \boldsymbol{x}_p + \boldsymbol{B}_p \boldsymbol{u} + \boldsymbol{C}_p d_p(t). \tag{16}$$

The hydraulic pitch servo is in principle a servo system represented by a state space model (17). The unmodeled dynamics and parametric uncertainties are represented as disturbance term as given in the following:

$$\begin{cases} \boldsymbol{A}_{p} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & -\frac{b_{L}}{J_{m\,b}} & \frac{D_{m}}{J_{m\,b\,i_{p}}} \\ 0 & -\frac{4\beta_{e}D_{m\,i_{p}}}{V_{p}} & -\frac{4\beta_{e}K_{cm}}{V_{p}} \end{bmatrix}, \boldsymbol{B}_{p} = \begin{bmatrix} 0 \\ 0 \\ \frac{4\beta_{e}K_{q}K_{u}}{V_{p}} \end{bmatrix} \\ \boldsymbol{C}_{p} = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}, J_{m\,b} = J_{m} + \frac{J_{b}}{i_{p}^{2}}; K_{cm} = K_{c} + c_{m} \end{cases}$$
(17)

## IV. POWER SMOOTHING CONTROL OF THE TIDAL TURBINE

The tidal pitch control is designed in a composite hierarchical manner that includes an upper level generator power smoothing controller and a low-level pitch angle tracking controller. It operates when the tidal speed is above rated. The generator power smoothing controller is designed to generate a suitable reference pitch angle that is employed to maintain the generator power at the rated value. In this section, a UDE-based robust power smoothing controller is proposed, which can handle model nonlinearity, uncertainty, and system disturbances. Due

#### A. Controller Synthesis

The generator output power is expressed as  $P_g = T_e \omega_g$ . Since  $\ell_{b_\beta} P_g \neq 0$  ( $\ell$  denotes the Lie derivative), the relative degree of generator power output is 1. Hence, the dynamics of the generator power can be formulated based on (9) as follows:

$$\begin{cases} \dot{P}_g = \ell_{g_\beta} P_g + \ell_{b_\beta} P_g \beta + \ell_{d_\beta} P_g + \dot{T}_e \omega_g \\ \ell_{g_\beta} P_g = g_\beta T_e; \ell_{b_\beta} P_g = b_\beta T_e; \ell_{d_\beta} P_g = d_\beta T_e \end{cases}$$
(18)

And the generator power dynamics is written as

$$\begin{cases} \dot{x} = g(x) + b\beta + d(x,t) \\ x = P_g, g(x) = \ell_{g_\beta} P_g; \\ b = \ell_{b_\beta} P_g; d(x,t) = \ell_{d_\beta} P_g + \dot{T}_e \omega_g \end{cases}$$
(19)

With the generator power dynamics developed in (19), the UDE-based power smoothing controller is synthesized with the control objective that the output power x asymptotically tracks the rated generator power  $x_r$  as closely as possible in spite of various model uncertainties and disturbances. The control input of the pitch angle is produced based on the tracking error between actual and the rated generator power.

The power tracking error is written as

$$e = x_r - x. \tag{20}$$

The desired error dynamics is designed as

$$\dot{e} = -K_1 e. \tag{21}$$

Combining (19)-(21) gives

$$\dot{e} = \dot{x}_r - \dot{x} = \dot{x}_r - g(x) - b\beta - d(x,t) = -K_1 e.$$
 (22)

According to the system dynamics in (19), the uncertain term d(x,t) can be estimated by using a filter with appropriate bandwidth as follows:

$$\hat{d}(x,t) = d(x,t)^* g_f(t) = (\dot{x} - g(x) - b\beta)^* g_f(t)$$
$$= L^{-1} \{G_f(s)\}^* (\dot{x} - g(x) - b\beta).$$
(23)

The low-pass filter  $G_f(s)$  is expressed as

$$G_f(s) = \frac{1}{1 + \tau s}.$$
(24)

Assuming the estimation error as  $\Delta d = d(x,t) - \hat{d}(x,t)$  and combining (22) and (23) yield

$$b\beta = \dot{x}_r - g(x) - L^{-1} \{G_f(s)\} * (\dot{x} - g(x) - b\beta) + K_1 e - \Delta d.$$
(25)

Following the procedures in [18], rearranging (25) leads to the UDE control design as follows:

$$\beta = b^{-1} \left\{ L^{-1} \left[ \frac{1}{1 - G_f(s)} \right] * (\dot{x}_r + K_1 e) - g(x) - L^{-1} \left[ \frac{sG_f(s)}{1 - G_f(s)} \right] * x \right\}.$$
(26)

Since the rated generator power is assumed as a constant  $\dot{x}_r = 0$  and the following equations are derived based on (24):

$$\begin{cases} \frac{1}{1 - G_f(s)} = 1 + \frac{1}{\tau s} \\ \frac{sG_f(s)}{1 - G_f(s)} = \frac{1}{\tau} \end{cases}.$$
 (27)

Then the control law in (26) is written as

$$\beta = b^{-1} \left\{ K_1 e - g(x) - \frac{1}{\tau} \left[ e + K_1 \int e(\xi) \, d\xi \right] \right\}.$$
 (28)

The control law in (28) has two parts: a model compensation term for canceling the known system dynamics and a local positive feedback loop behaving like a proportional–integral controller. The error feedback gain can be chosen arbitrarily large to attenuate the high-frequency components of the uncertainty and disturbances. It is worth noting that the control gain b also needs to be calculated by using the control input, which may lead to algebraic loop during the control implementations. A practical solution to this problem is to use the control input at previous time instants to compute the control gain at the current time instant when the sampling rate in the digital implementation is chosen highly faster than the variation rate of the control input.

#### B. Estimation of Tidal Stream Speeds

The control law in (28) is implemented assuming that all the states and the tidal stream speed are available for feedback. However, in practice, the tidal stream speed is not always directly measurable or is very expensive to measure. Thus, the UDE controller (28) adopts an estimation of the tidal speed signal to construct the control law.

Assuming an ideal drivetrain model, i.e.,  $\Delta \omega_t = \Delta \dot{\omega}_t = 0$ , the turbine torque is estimated based on (8) as follows:

$$\hat{T}_{t} = L^{-1} \left\{ G_{f}\left(s\right) \right\} * \left\{ \left( \frac{J_{t}}{i_{g}} + J_{g}i_{g} \right) \dot{\omega}_{g} + \left( \frac{k_{t}}{i_{g}} + k_{g}i_{g} \right) \omega_{g} + T_{e} \cdot i_{g} \right\}.$$
(29)

By rearranging (1), the turbine torque is also represented as

$$\hat{T}_t = \frac{\rho \pi R^2 \hat{v}^3 i_g C_p}{2\omega_g}.$$
(30)

Thus the tidal stream speed is readily estimated as

$$\hat{v} = \left(\frac{2\omega_g \hat{T}_t}{\rho \pi R^2 i_g C_p}\right)^{\frac{1}{3}}.$$
(31)

As indicated in (31), the estimation of tidal stream speeds needs the information of power coefficient  $C_p$  that depends on the blade pitch angle and TSR, and is thus not always known at the current time instant. A practical solution to this problem is to use the power coefficient  $C_p$  calculated at a previous time instant to calculate the tidal stream speed at the current time instant since the tidal turbine power coefficient changes much slower than the turbine pitch system and tidal streams. In addition, the calculation in (31) can also be made accurate enough when the sampling rate in the online digital implementation is chosen highly faster than the variation rate of the power coefficient. Then the UDE-based robust control law for power smoothing in (28) can be reformulated as

$$\beta = \hat{b}^{-1} \left\{ K_1 e - g(x) - \frac{1}{\tau} \left[ e + K_1 \int e(\xi) \, d\xi \right] \right\}.$$
 (32)

Actually, the pitch servo system may not accurately achieve the reference or the desired pitch angle in (32) due to the servo performance limitations. The pitch angle control law in (32) should be rewritten as the desired or the reference pitch angle

$$\beta_{r} = \hat{b}^{-1} \left\{ K_{1}e - g(x) - \frac{1}{\tau} \left[ e + K_{1} \int e(\xi) \,\mathrm{d}\xi \right] \right\}$$
(33)

where  $\beta$  is rearranged as  $\beta_r$  and  $\beta_r = \beta + e_{\beta}$ .

## V. PITCH ANGLE CONTROL

In this section, the UDE-based pitch angle controller is designed based on (16) to have the pitch servo system to asymptotically track the derived reference pitch angle trajectory in (33) as closely as possible, while the uncertainty and disturbance are completely compensated and rejected.

In order for the closed-loop pitch servo system to satisfy the desired pitch angle tracking performances, the following stable reference model in a controllable canonical is selected:

$$\dot{\boldsymbol{x}}_m = \boldsymbol{A}_m \boldsymbol{x}_m + \boldsymbol{B}_m c(t). \tag{34}$$

The control objective is thus to track the reference state vector  $\boldsymbol{x}_m$  and the tracking error  $\boldsymbol{e}_p(t) = \boldsymbol{x}_m - \boldsymbol{x}_p$  satisfies the ideal dynamics

$$\dot{\boldsymbol{e}}_p(t) = (\boldsymbol{A}_m + \boldsymbol{K}_2)\boldsymbol{e}_p(t). \tag{35}$$

Combining (16), (34), and (35) results in

$$\boldsymbol{B}_{p}\boldsymbol{u} = \boldsymbol{A}_{m}\boldsymbol{x}_{p} + \boldsymbol{B}_{m}\boldsymbol{c}(t) - \boldsymbol{A}_{p}\boldsymbol{x}_{p} - \boldsymbol{K}_{2}\boldsymbol{e}_{p}(t) - \boldsymbol{C}_{p}\boldsymbol{d}_{p}(t).$$
(36)

According to the pitch system dynamics described by (16), the lumped disturbance term  $d_p(t)$  in (36) is represented as

$$C_p \hat{d}_p(t) = (\dot{\boldsymbol{x}}_p - \boldsymbol{A}_p \boldsymbol{x}_p - \boldsymbol{B}_p \boldsymbol{u}) * g_f(t)$$
$$= L^{-1} \{G_f(s)\} * (\dot{\boldsymbol{x}}_p - \boldsymbol{A}_p \boldsymbol{x}_p - \boldsymbol{B}_p \boldsymbol{u}). \quad (37)$$

Substituting the disturbance term  $d_p(t)$  in (36) with its estimate in (37) yields

$$\boldsymbol{B}_{p}\boldsymbol{u} = \boldsymbol{A}_{m}\boldsymbol{x}_{p} + \boldsymbol{B}_{m}\boldsymbol{c}(t) - \boldsymbol{A}_{p}\boldsymbol{x}_{p} - \boldsymbol{K}_{2}\boldsymbol{e}_{p}(t)$$
$$- (\dot{\boldsymbol{x}}_{p} - \boldsymbol{A}_{p}\boldsymbol{x}_{p} - \boldsymbol{B}_{p}\boldsymbol{u}) * g_{f}(t). \qquad (38)$$

Hence, the UDE-based control law is formulated as

$$u = -\boldsymbol{B}_{p}^{+} \left\{ \boldsymbol{A}_{p}\boldsymbol{x}_{p} + L^{-1} \left[ \frac{sG_{f}(s)}{1-G_{f}(s)} \right] * \boldsymbol{x}_{p} + L^{-1} \left[ \frac{1}{1-G_{f}(s)} \right] (\boldsymbol{A}_{m}\boldsymbol{x}_{p} + \boldsymbol{B}_{m}c(t) - \boldsymbol{K}_{2}\boldsymbol{e}_{p}(t)) \right\}.$$
(39)

Substituting (38) into (16) results in

$$\dot{\boldsymbol{x}}_{p} = \boldsymbol{A}_{m}\boldsymbol{x}_{p} + \boldsymbol{B}_{m}c(t) - \boldsymbol{K}_{2}\boldsymbol{e}_{p}(t) - \boldsymbol{C}_{p}d_{p} * g_{f}(t) + \boldsymbol{C}_{p}d_{p}.$$
(40)

Substituting (34) into (40) and rearranging the resulting equations yield

$$\begin{cases} \boldsymbol{X}_{p}(s) = \boldsymbol{H}_{m}(s)C(s) + \boldsymbol{H}_{d}(s)\boldsymbol{B}_{p}\boldsymbol{B}_{p}^{+}\boldsymbol{C}_{p}\left[1 - G_{f}\left(s\right)\right]d_{p} \\ \boldsymbol{H}_{m}(s) = (s\boldsymbol{I} - \boldsymbol{A}_{m})^{-1}\boldsymbol{B}_{m} \\ \boldsymbol{H}_{d}(s) = \left[1 - G_{f}\left(s\right)\right]\left[s\boldsymbol{I} - (\boldsymbol{A}_{m} + \boldsymbol{K}_{2})\right]^{-1} \end{cases}$$
(41)

As revealed in (41), the UDE-based pitch angle controller has two-degree-of-freedom nature that allows the decoupled design of the reference model and the filter. It is clear that for any bounded uncertain term  $d_p$ , if the low-pass filter  $G_f(s)$  is chosen to cover the whole frequency content of  $d_p$ , the actual state trajectory of the pitch servo system will be only determined by the reference input c(t).

The actual pitch angle tracking error is then obtained by combining (34) and (41) as

$$\boldsymbol{E}_{p}(s) = -[s\boldsymbol{I} - (\boldsymbol{A}_{m} + \boldsymbol{K}_{2})]^{-1}\boldsymbol{B}_{p}\boldsymbol{B}_{p}^{+}\boldsymbol{C}_{p}\left[1 - G_{f}\left(s\right)\right]d_{p}.$$
(42)

As aforementioned, the low-pass filter  $G_f(s)$  is strictly proper and stable with  $G_f(0) = 1$ ,  $d_p$  is bounded, and  $[sI - (A_m + K_2)]^{-1}$  is designed to be stable. Then the steadystate error will converge to zero in finite time by applying the final value theorem [20], i.e.,  $\lim_{t\to\infty} e_p(t) = \lim_{s\to 0} sE_p(s) =$ 0. By substituting (27) into (39) and considering (34) and (35), the UDE-based control law in (39) is reformulated as

$$u = -\boldsymbol{B}_{p}^{+} \left\{ \left( \boldsymbol{A}_{p} + \boldsymbol{A}_{m} \right) \boldsymbol{x}_{m} + \boldsymbol{B}_{m} c(t) + \frac{1}{\tau} \begin{bmatrix} \left( 2\boldsymbol{x}_{m} - \boldsymbol{e}_{p} \right) - \left( \boldsymbol{A}_{p} + \boldsymbol{A}_{m} + \boldsymbol{K}_{2} \right) \tau \boldsymbol{e}_{p} \\ - \left( \boldsymbol{A}_{m} + \boldsymbol{K}_{2} \right) \int_{0}^{t} \boldsymbol{e}_{p} \left( \xi \right) d\xi \end{bmatrix} \right\}.$$
(43)

It is clear that the control law (48) is formulated by using the system state, the reference model, the low-pass filter, and the error feedback gain.

#### VI. STABILITY ANALYSIS

The overall stability of the entire tidal pitch angle control system can be analyzed as follows.

For the power smoothing control loop, by using the relationship  $\beta = \beta_r - e_\beta$ , substituting (33) into the error dynamics (22) and considering (27), the power tracking error dynamics in (22) is reformulated as

$$\dot{e} = -K_1 e - \dot{b}\beta + \dot{b}e_\beta - \Delta d \tag{44}$$

where  $\Delta d = L^{-1}[1 - G_f(s)] * d(x, t)$ .

For the pitch angle control loop, by considering the estimated lumped disturbance term  $d_p(t)$  in (37), the pitch angle tracking error dynamics in (35) becomes

$$\dot{\boldsymbol{e}}_p(t) = (\boldsymbol{A}_m + \boldsymbol{K}_2)\boldsymbol{e}_p(t) - \boldsymbol{C}_p \Delta d_p.$$
(45)

The following defines the Lyapunov function candidates to analyze the stability of the overall tidal pitch control system:

$$\begin{cases} V(t) = V_1(t) + V_2(t) \\ V_1(t) = \frac{1}{2}e^2 \\ V_2(t) = e_p^{\mathrm{T}}(t)Pe_p(t) \end{cases}$$
(46)

Differentiating  $V_1(t)$  with respect to time along with the error dynamics in (34) gives

$$\dot{V}_1(t) = e\dot{e} = -K_1 e^2 - e\tilde{b}\beta + e\hat{b}e_\beta - e\Delta d.$$
(47)

By applying Young's inequality to (47), the following inequality holds:

$$\dot{V}_{1}(t) \leq -K_{1}e^{2} + \frac{1}{2}e^{2} + \frac{1}{2}\left(\hat{b}e_{\beta} - \tilde{b}\beta - \Delta d\right)^{2} \\ = \left(\frac{1}{2} - K_{1}\right)e^{2} + \frac{1}{2}\left(\hat{b}e_{\beta} - \tilde{b}\beta - \Delta d\right)^{2}.$$
 (48)

The time derivative of  $V_2(t)$  can be obtained as

$$\dot{V}_{2}(t) = \boldsymbol{e}_{p}^{\mathrm{T}}(t) \left[ (\boldsymbol{A}_{m} + \boldsymbol{K}_{2})^{\mathrm{T}} \boldsymbol{P} + \boldsymbol{P}(\boldsymbol{A}_{m} + \boldsymbol{K}_{2}) \right]$$
$$\times \boldsymbol{e}_{p}(t) - 2\boldsymbol{e}_{p}^{\mathrm{T}}(t) \boldsymbol{P} \boldsymbol{C}_{p} \Delta d_{p}.$$
(49)

By using the following inequalities:

$$\begin{cases} \boldsymbol{e}_{p}^{\mathrm{T}}(t) \left[ \left(\boldsymbol{A}_{m} + \boldsymbol{K}_{2}\right)^{\mathrm{T}} \boldsymbol{P} + \boldsymbol{P}(\boldsymbol{A}_{m} + \boldsymbol{K}_{2}) \right] \boldsymbol{e}_{p}(t) \\ \leq \lambda_{\max} \left[ \left(\boldsymbol{A}_{m} + \boldsymbol{K}_{2}\right)^{\mathrm{T}} \boldsymbol{P} + \boldsymbol{P}(\boldsymbol{A}_{m} + \boldsymbol{K}_{2}) \right] \boldsymbol{e}_{p}^{\mathrm{T}}(t) \boldsymbol{e}_{p}(t) \\ -2\boldsymbol{e}_{p}^{\mathrm{T}}(t) \boldsymbol{P} \boldsymbol{C}_{p} \Delta d_{p} \leq \boldsymbol{e}_{p}^{\mathrm{T}}(t) \boldsymbol{e}_{p}(t) + \| \boldsymbol{P} \boldsymbol{C}_{p} \Delta d_{p} \|^{2} \\ \lambda_{\min}\left(\boldsymbol{P}\right) \boldsymbol{e}_{p}^{\mathrm{T}}(t) \boldsymbol{e}_{p}(t) \leq V_{2}\left(t\right) \leq \lambda_{\max}\left(\boldsymbol{P}\right) \boldsymbol{e}_{p}^{\mathrm{T}}(t) \boldsymbol{e}_{p}(t) \end{cases}$$
(50)

It is natural to derive that

$$\dot{V}_{2}(t) \leq \left\{ \lambda_{\max} \left[ (\boldsymbol{A}_{m} + \boldsymbol{K}_{2})^{\mathrm{T}} \boldsymbol{P} + \boldsymbol{P} (\boldsymbol{A}_{m} + \boldsymbol{K}_{2}) \right] \\ + 1 \right\} \boldsymbol{e}_{p}^{\mathrm{T}}(t) \boldsymbol{e}_{p}(t) \\ + \| \boldsymbol{P} \boldsymbol{C}_{p} \Delta d_{p} \|^{2} \leq \frac{V_{2}(t)}{\lambda_{\min}(\boldsymbol{P})} \left\{ \lambda_{\max} \left[ (\boldsymbol{A}_{m} + \boldsymbol{K}_{2})^{\mathrm{T}} \boldsymbol{P} \right] \\ + \left. \boldsymbol{P} (\boldsymbol{A}_{m} + \boldsymbol{K}_{2}) \right] + 1 \right\} \\ + \| \boldsymbol{P} \boldsymbol{C}_{p} \Delta d_{p} \|^{2}.$$
(51)

By considering (46), (47), and (51), the time derivative of the Lyapunov function V(t) can be obtained as

$$\begin{split} \dot{V}(t) &= \dot{V}_{1}(t) + \dot{V}_{2}(t) \leq \frac{V_{2}(t)}{\lambda_{\min}(\boldsymbol{P})} \\ &\times \left\{ \lambda_{\max} \left[ (\boldsymbol{A}_{m} + \boldsymbol{K}_{2})^{\mathrm{T}} \boldsymbol{P} + \boldsymbol{P}(\boldsymbol{A}_{m} + \boldsymbol{K}_{2}) \right] + 1 \right\} \\ &+ \|\boldsymbol{P}\boldsymbol{C}_{p}\Delta d_{p}\|^{2} + \left(\frac{1}{2} - K_{1}\right) e^{2} \\ &+ \frac{1}{2} \left( \hat{b}e_{\beta} - \tilde{b}\beta - \Delta d \right)^{2} \\ \leq - (2K_{1} - 1) V_{1}(t) - \\ &\left\{ -\frac{\left\{ \lambda_{\max} \left[ (\boldsymbol{A}_{m} + \boldsymbol{K}_{2})^{\mathrm{T}} \boldsymbol{P} + \boldsymbol{P}(\boldsymbol{A}_{m} + \boldsymbol{K}_{2}) \right] + 1 \right\} \right\} \\ &\times V_{2}(t) \\ &+ \|\boldsymbol{P}\boldsymbol{C}_{p}\Delta d_{p}\|^{2} + \frac{1}{2} \left( \hat{b}e_{\beta} - \tilde{b}\beta - \Delta d \right)^{2}. \end{split}$$
(52)

By defining

$$\begin{cases} \gamma_{1} = \min \begin{cases} (2K_{1} - 1), \\ -\frac{\{\lambda_{\max}[(\boldsymbol{A}_{m} + \boldsymbol{K}_{2})^{\mathrm{T}} \boldsymbol{P} + \boldsymbol{P}(\boldsymbol{A}_{m} + \boldsymbol{K}_{2})] + 1\} \\ \lambda_{\min}(\boldsymbol{P}) \end{cases} \end{cases} \\ \gamma_{2} = \|\boldsymbol{P}\boldsymbol{C}_{p}\Delta d_{p}\|^{2} + \frac{1}{2} \left(\hat{b}\boldsymbol{e}_{\beta} - \tilde{b}\beta - \Delta d\right)^{2} \end{cases}$$
(53)

it is natural to derive that

$$\dot{V}(t) = -\gamma_1 V(t) + \gamma_2.$$
(54)

By solving (54), one obtains

$$0 \le V(t) \le V(0) \exp(-\gamma_1 t) + \frac{\gamma_2}{\gamma_1} \left[1 - \exp(-\gamma_1 t)\right].$$
 (55)

Since  $\gamma_1$  and  $\gamma_2$  are positive and bounded due to the local boundness of the pitch angle and the selection of  $K_1$ ,  $K_2$ , and P, V(t) will be bounded by  $\gamma_2/\gamma_1$  when  $t \to \infty$ . Thus, the power tracking error  $e(\infty) < \sqrt{\frac{2\gamma_2}{\gamma_1}}$ , which can be readily reduced by increasing the feedback gain  $K_1$  and designing a suitable low-pass filter  $G_f(s)$  to reduce the estimation errors. Then the closed-loop control system is stable, and the asymptotic rated generator power tracking and disturbance rejection are achieved in finite time [19]. We mention that the generator power quality and transient stability may be further improved when considering fault ride-through schemes like wind turbines [21].

## VII. VALIDATIONS AND DISCUSSIONS

In this section, the feasibility and effectiveness of the proposed UDE-based power smoothing controller and the pitch angle controller are thoroughly evaluated based on a demonstrative 600 kW tidal turbine with geared transmission and variable pitch control. The proposed tidal pitch system is applicable for general tidal turbines.

The rated tidal stream speed for the pitch angle control is 1.8 m/s. The reference pitch angle is generated by using the control law in (33) and the pitch system is controlled by the



Fig. 5. Responses to the reference square pitch signal.



Fig. 6. Responses to the reference sinusoidal pitch signal.

UDE-based control law in (43). In order to achieve a good attenuation ratio of the UDE control, the time constant  $\tau$  in the low-pass filter  $G_f(s)$  is chosen as a small positive value of 0.001 s to ensure that the filter bandwidth covers the spectrum of uncertainties and disturbances. The constant error feedback gain  $K_1$  is chosen to be 0.67, and the error feedback gain matrix  $K_2$  is chosen to be diag  $\{1.2 \times 10^3, 1.6 \times 10^3, 3.4 \times 10^4\}$ . In addition, memory blocks are used to deal with the algebraic loop and unknown power coefficient as mentioned in Section IV.

The simulation methods are currently available in Simscape Power Systems Specialized Technology in Simulink to model turbine-based energy conversion systems. The model is discretized at 5 ms and the dynamics resulting from pitch control system and power system interactions are preserved.

The results of the proposed novel pitch system are compared with that of an existing pitch system [8] to evaluate the generator power qualities and speed control performances under different operation conditions. The control efficiency of the proposed UDE-based pitch angle controller is also compared with a conventional proportional–integral–derivative (PID) controller. To compare these two controllers fairly, their parameters are well-tuned to produce similar pitch angle tracking performance. The PID parameters are respectively chosen as  $4.3 \times 10^8$ , 0.01, and  $1.2 \times 10^5$ .

#### A. Pitch System Dynamics

As shown in Fig. 5, the rising time and peak time of the proposed UDE controller are relatively lower than that of the PID controller that is commonly used in most of the commercial wind or tidal turbines. This means that the UDE control responds faster and can help to further improve the pitch system dynamics in comparison with PID control.



Fig. 7. Tidal stream speed and its estimates.



Fig. 8. Pitch angle variations.

As shown in Fig. 6, the pitch angle tracking errors are almost kept zero by using both the PID and UDE controllers, which indicate that these two controllers can guarantee the stability of the closed-loop pitch servo system. Compared with the PID controller, the UDE-based controller maintains lower tracking error and thus better tracking accuracy. This is due to the fact that the UDE controller uses more derivative information than the PID controller.

### *B. Pitch Control Performances Under Normal Tidal Stream Condition*

As shown in Fig. 7, the real-world typical tidal stream speed data (around 1.8 m/s) is used as external input to the tidal turbine system to test the proposed pitch system. The speed signals are of crucial importance to the tidal turbine and determine its operating regions. Around the tidal speed of 1.8 m/s, the proposed pitch system will be activated to generate suitable pitch angles to smooth generator power. The tidal stream speed can also be accurately approximated by using the speed estimation (29)–(31) without using any tidal speed sensors, which will largely reduce system cost.

As illustrated in Fig. 8, the two pitch systems are activated during above the rated tidal stream speed conditions to regulate the tidal power generations. The pitch angle from the proposed pitch system varies between  $0^{\circ}$  and  $2.8^{\circ}$  while the pitch angle of the existing pitch system [8] varies in a narrower range between  $0^{\circ}$  and  $2.2^{\circ}$ . Thus, it is obvious that the proposed pitch system generates pitch angle outputs in a wider range and can therefore execute more pitch actions than the existing pitch system.



Fig. 9. Generator power variations.



Fig. 10. Tidal stream speed and its estimates.

As shown in Fig. 9, by using the proposed pitch system, the averaged generator power is also smoothed and maintained around the rated value of 600 kW despite of the uncertainty and disturbances from the system dynamics and input signal. On the other hand, the generator power varies more significantly between 500 and 700 kW when the existing pitch system is used. This comparison result indicates that the proposed pitch system is more capable of smoothing the generator power and maintaining the rated value than the existing pitch system [8].

## C. Pitch Control Performance Under Sudden Large Spring Tides

As shown in Fig. 10, the measured real-world sudden large spring tides increase from 0 to around 3.5 m/s which is about two times the rated tidal speed. The extreme speed of 3.5 m/s continues for about 4 s and can be readily used to evaluate the control performances of the proposed pitch system. The estimated tidal stream speed also closely matches the real speed data, which clearly demonstrates the effectiveness of the estimation algorithm in Section IV-B.

As illustrated in Fig. 11, the pitch angles vary between  $0^{\circ}$  and  $10^{\circ}$  and have positive relationship with the tidal stream speed as shown in Fig. 10. The pitch angle generated from the proposed pitch system is relatively larger and varies more significantly than that from the existing pitch system. Therefore, the proposed pitch system is more effective in producing necessary pitch angle control actions to regulate the generator power and speed during the sudden large spring tidal conditions.

As shown in Figs. 12 and 13, the generator speed and power suddenly increase to more than 160 rad/s and 750 kW,





Fig. 12. Generator speed variations.



Fig. 13. Generator power variations.

respectively, during the sudden large spring tides, causing an oscillation on the dc-bus voltage and the grid. During this extreme condition, the pitch systems are timely activated to regulate the generator speed and power at their set points. The generator speed and power can be regulated around the rated values and the fluctuations can be more smoothed when using the proposed pitch system while the generator speed and power fluctuate more significantly when the existing pitch system [8] is applied. This is largely due to the fact that the proposed pitch system has much faster and more accurate pitch control performances as compared with the existing pitch system that has relatively inaccurate pitch actuations due to the inevitably imprecise motion transformations and inherent frictions in the rack and pinion mechanism. As a consequence, the proposed pitch system is more effective in maintaining the rated generator speed and power even in the presence of sudden large spring tides as compared with the existing pitch system.

As indicated in the aforementioned results, the proposed pitch system can potentially improve tidal energy efficiency

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and power leveling over a wide range of tidal stream speeds like wind turbine pitch systems [5], [22].

#### VIII. CONCLUSION

This paper presented the systematic design, dynamics modeling, and UDE-based pitch control of a novel tidal pitch system based on hydraulic servo and bevel geared transmission. The pitch system had a compact and triangular structure, and its dynamics model considers model uncertainties and external disturbances that were readily estimated and compensated by the proposed UDE-based control law. The UDE pitch control was designed in a composite hierarchical manner that included an upper level generator power smoothing controller and a low level pitch angle tracking controller. The UDE-based robust power smoothing controller was proposed for accurate and stable operations of the power generation, while the UDE-based pitch angle controller was designed to have the pitch system to asymptotically track the derived reference pitch angle trajectory. The feasibility and effectiveness of the proposed pitch system and UDE controller was evaluated through simulation studies based on a 600 kW variable speed, variable pitch tidal turbine. The results demonstrated that the UDE control-based pitch system had excellent dynamic characteristics and higher pitch angle tracking accuracy as compared with the conventional PID control method. The proposed tidal pitch system is easy to install on real tidal turbines. Future work is to build an experimental test rig and conduct experiment tests to verify its effectiveness under more complicated situations.

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